

Timing attacks

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Minerva attack can recover private keys from smart cards, cryptographic libraries

Older Athena IDProtect smart cards are impacted, along with the WolfSSL, MatrixSSL, Crypto++, Oracle SunEC, and Libcrypt crypto libraries.



By [Catalin Cimpanu](#) for [Zero Day](#) | October 3, 2019 -- 12:54 GMT (13:54 BST) | Topic: [Security](#)



[ZDNet article](#)

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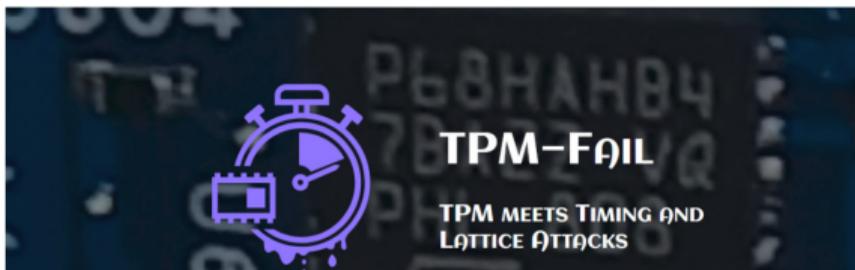
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TPM-FAIL lets attackers steal private keys from TPMs. Attacks take from minutes to a few hours.



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ELLIPTISCHE KURVEN

Minerva-Angriff zielt auf zertifizierte Krypto-Chips

Forscher konnten zeigen, wie sie mit einem Timing-Angriff die privaten Schlüssel von Signaturen mit elliptischen Kurven auslesen konnten. Verwundbar sind Chips, deren Sicherheit eigentlich zertifiziert wurde.

4. Oktober 2019, 13:41 Uhr, Hanno Böck



is Hollar, Wikimedia Commons

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Timing attacks are not a new phenomenon

Password recovery if server compares letter by letter:

Try AAA,

Timing attacks are not a new phenomenon

Password recovery if server compares letter by letter:

Try AAA, BBB,

Timing attacks are not a new phenomenon

Password recovery if server compares letter by letter:

Try AAA, BBB, CCC, ...

Timing attacks are not a new phenomenon

Password recovery if server compares letter by letter:

Try AAA, BBB, CCC, . . . , III takes slightly longer to fail.

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Password recovery if server compares letter by letter:

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Password recovery if server compares letter by letter:

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⋮

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Try IKA, IKB, IKC, . . . , IKV takes slightly longer to fail.

⋮

Password is IKVROCKS.

1974: Exploit developed by Alan Bell for TENEX operating system.

Exponentiation with secret exponent (RSA, DH)

Compute c^d given c and d .

```
n = 1000001
```

```
d = 12473
```

```
c = 41241
```

```
l = d.nbits()
```

```
D = d.bits()
```

```
m = c
```

```
for i in range(l-2, -1, -1):
```

```
    m = m^2 % n
```

```
    if D[i] == 1:
```

```
        m = m * c % n
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```
print(m)
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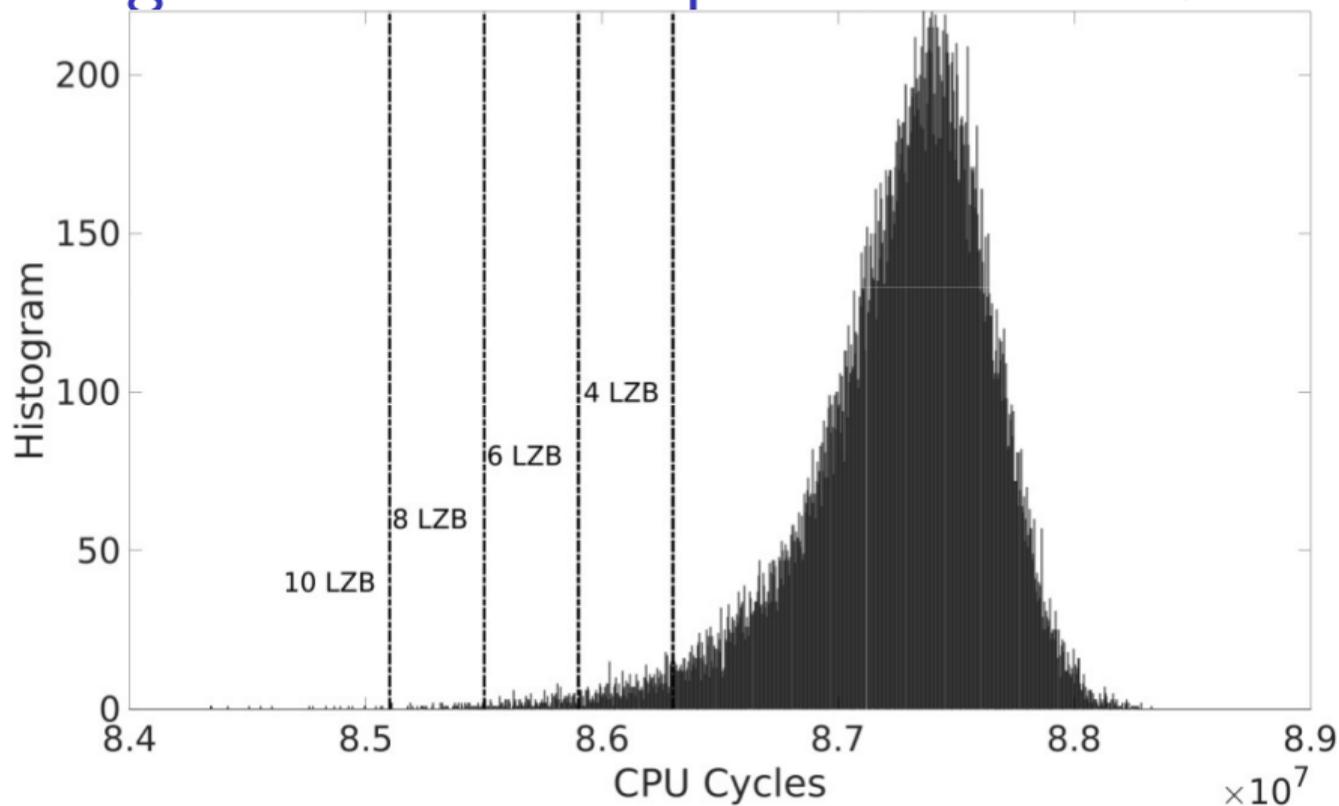
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```

```
    if D[i] == 1: # branch depends on d
```

```
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```

```
print(m)
```

Timings of scalar multiplication on NIST P-256



(Picture from [TPM-Fail](#))

Other exponentiation methods

- The timing variation depends strongly on the length of the scalar/exponent.
- Very sparse or very dense scalars will be miscategorized.
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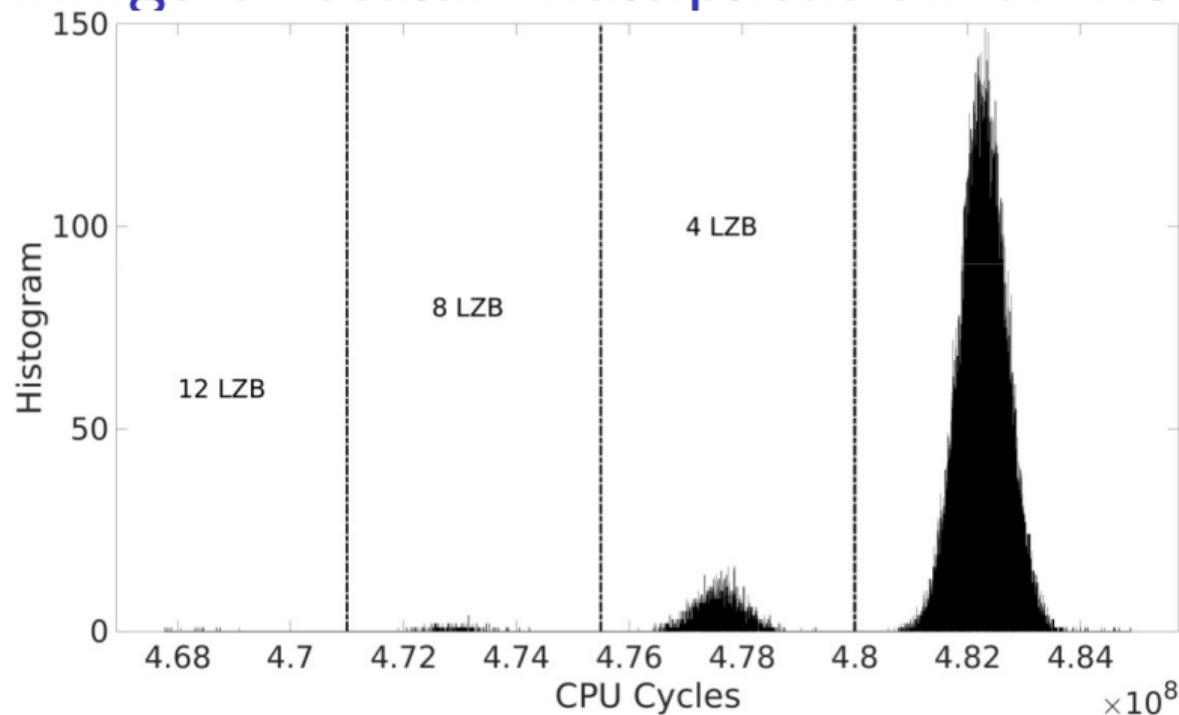
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Precompute c , c^2 , and c^3 .

$$c^{14019} = \left(\left(\left(\left(\left((c^3)^4 \cdot c \right)^4 \cdot c^2 \right)^4 \cdot c^3 \right)^4 \right)^4 \right)^4 \cdot c^3.$$

Same number of squarings, 4 instead of 7 multiplications.

Timings of scalar multiplication on NIST P-256



Larger windows reduce the variability through branching but accentuate the length.

(Picture from [TPM-Fail](#))

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 - TPM-Fail: TPM meets Timing and Lattice Attacks
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<https://tpm.fail/>
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With just a small bias in the nonces (one-time scalars) the secret signing key leaks.

- Lots of libraries, smart cards, and TPMs affected.
- Even worse: hyperthreading attacks, cache-timing attacks, etc. give more fine-grained timing information \Rightarrow more exploits.

Constant-time exponentiation

```
n = 1000001
d = 12473
c = 41241
l = n.nbits()
D = d.digits(2, padto = l)
m = 1 # so initial squarings don't matter
for i in range(l-1, -1, -1): # fixed-length loop
    m = m^2 % n
    h = m * c % n
    m = (1 - D[i]) * m + D[i] * h # selection by arithmetic
print(m)
```

This costs 1 multiplication per bit, so as slow as worst case.

Interplay with elliptic-curve formulas

- We can translate this to scalar multiplication on elliptic curves: Initialize with the neutral element, for every bit compute a doubling and an addition.
- Formulas for addition on Weierstrass curves have exceptions for adding ∞ , so initialization at ∞ does not work.
- Edwards curves have a complete addition law, **easy** to double or add the neutral element $(0, 1)$.
- The Montgomery ladder has a similar data flow, but the costs per bit of the scalar are **less** than one addition plus one doubling for Montgomery curves.

For more see <https://ecchacks.cr.yp.to>.