Cryptology, homework sheet 5

Due 19 October 2021, 13:15

Team up in groups of two or three to hand in your homework. We do not have capacity to correct all homeworks individually.

For this sheet you can use Sage for exponentiations modulo large numbers and gcds. Make sure to document what you type and what the answers are.

- 1. Bob uses public key (n, e) = (396553, 17). His secret key is a CRT key using p = 541 and q = 733.
 - (a) Compute the full secret key (n, p, q, d_p, d_q, u) .

1.5 points

- (b) Decrypt ciphertext c=234040 using the CRT method and verify your result by reencrypting it.
 - Make sure to document your computation, i.e., state the values for c_p, m_p, \ldots Note that there was a typo on the slides in the video for computing m; the slides have been fixed.
- 2. This exercise is about factoring.
 - (a) Use the p-1 method to factor n=396553 with basis a=8 and exponent s=lcm(1,2,3,4,5,6,7,8,9,10,11,12). Make sure to state the value for s and the result of the exponentiation modulo n. Determine both factors of n.
 - (b) The factorization of 540 is $540 = 2^2 \cdot 3^3 \cdot 5$ and that of 732 is $732 = 2^2 \cdot 3 \cdot 61$. Explain why the factorization in (a) was successful.

Hint: Check whether a = 2 would have worked.

3.5 points